

1	(i)	<p>grad AB = $\frac{7-1}{4-2}$ oe or 3 $y - 7 = \text{their } m(x - 4)$ or $y - 1 = \text{their } m(x - 2)$</p> <p>$y = 3x - 5$ oe</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>or use of $y = \text{their gradient } x + c$ with coords of A or B or M2 for $\frac{y-1}{7-1} = \frac{x-2}{4-2}$ o.e.</p> <p>accept equivalents if simplified eg $3x - y = 5$ allow B3 for correct eqn www</p>	<p>allow step methods used</p> <p>or eg M1 for $7 = 4m + c$ and $1 = 2m + c$ then M1 for correctly finding one of m and c</p> <p>allow A1 for $c = -5$ oe if $y = 3x + c$ oe already seen</p> <p>B2 for eg $y - 1 = 3(x - 2)$</p>
1	(ii)	<p>showing grad BC = $\frac{2-1}{-1-2} = -\frac{1}{3}$ oe and $-1/3 \times 3 = -1$ or grad BC is neg reciprocal of grad AB, [so 90°]</p> <p><u>or</u> for finding AC or AC^2 independently of AB and BC</p> <p>for correctly showing $AC^2 = BC^2 + AB^2$ oe</p>	<p>B1</p> <p>B1</p> <p><u>or</u> B1</p> <p>B1</p>	<p>may be calculation or showing on diagram</p> <p>may be earned for statement / use of $m_1 m_2 = -1$ oe, even if first B1 not earned</p> <p>for B1+B1, must be fully correct, with 3 as gradient in (i)</p> <p><u>or</u> working needed such as $AC^2 = 5^2 + 5^2 = 50$</p> <p>working needed using correct notation such as $BC^2 = 3^2 + 1^2 = 10$; $AB^2 = 6^2 + 2^2 = 40$, $40 + 10 = 50$ [hence $AC^2 = BC^2 + AB^2$]</p>	<p>eg allow 2nd B1 for statement grad BC = $-1/3$ with no working if first B1 not earned</p> <p>condone any confusion between squares and square roots etc for first B1 and for two M1s eg $AC = 25 + 25 = \sqrt{50}$</p> <p>accept eg 3 and 1 shown on diagram and $BC^2 = 10$ etc</p> <p>0 for eg $\sqrt{40} + \sqrt{10} = \sqrt{50}$</p>

		<p><u>or</u> finding equation of line through C perpendicular to AB ($y = -\frac{1}{3}x + \frac{5}{3}$ oe)</p> <p>showing B is on this line either by substitution or finding intersection of this line with AB</p> <p>$BC = \sqrt{3^2 + 1^2}$ or $\sqrt{10}$ $AB = \sqrt{6^2 + 2^2}$ or $\sqrt{40}$ or $2\sqrt{10}$</p> <p>Area = 10 [square units] <u>or</u> area under AC – area under AB – area under BC</p> <p>at least two of 22.5, 8 and 4.5 oe Area = 10 [square units]</p>	<p><u>or</u> B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p><u>or</u> M1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>eg B1 for $x + 3y = 5$</p> <p>or B1 for finding the equation of the line through B and C as $y = -\frac{1}{3}x + \frac{5}{3}$ oe and B1 for using condition for perp lines and showing true</p> <p>for both M1s accept unsimplified equivs</p> <p>must be simplified to 10</p> <p>must be simplified to 10</p>	<p>for both M1s accept unsimplified equivs</p> <p>mark equivalently for other valid methods, eg trapezium – 2 triangles method, omitting below $y = 1$: $\frac{1}{2} \times 7 \times 5 - (\frac{1}{2} \times 3 \times 1 + \frac{1}{2} \times 2 \times 6)$ $= 17.5 - (1.5 + 6)$</p>
--	--	---	--	---	---

1	(iii)	<p>(1.5, 4.5) oe</p> <p>angle in semicircle oe is a right-angle [so B is on circle] and must mention AC as diameter or D as centre [hence A, B, C all same distance from D]</p>	<p>2</p> <p>E1</p> <p>[3]</p>	<p>B1 each coordinate</p> <p>or '[since $b = 90^\circ$,] ABC are three vertices of a rectangle. D is the midpoint of one diagonal <u>and</u> so D is the centre of the rectangle <u>or</u> the diagonals of a rectangle are equal and bisect each other, [hence $DA = DB = DC$]</p> <p>or condone showing that line from D to mid point of AB is perp to AB, so DBA is isos [hence $DB = DA = DC$] [or equiv using DBC]</p>	<p>E0 for just stating 'D is midpt of the hypotenuse of a rt angled triangle ABC so DAB is isos' without showing that it is</p> <p>isw eg wrong calcn of radius</p> <p>NB some wrongly asserting that ABC is isos</p>
---	-------	---	-------------------------------	--	---

2	7	<p>2</p> <p>condone $y = 7$ or $(5, 7)$;</p> <p>M1 for $\frac{k - (-5)}{5 - 1} = 3$ or other correct use of gradient eg triangle with 4 across, 12 up</p>	<p>condone omission of brackets;</p> <p>or M1 for correct method for eqn of line and $x = 5$ subst in their eqn and evaluated to find k;</p> <p>or M1 for both of $y - k = 3(x - 5)$ oe and $y - (-5) = 3(x - 1)$ oe</p>
---	---	---	--

3	$y = 5x + 3$	3 M2 for $y - 13 = 5(x - 2)$ oe or M1 for $y = 5x [+ k]$ [$k =$ letter or number other than -4] and M1 for $13 =$ their $m \times 2 + k$	or M1 for $y - b = 5(x - a)$ with wrong a, b or for $y - 13 =$ their $5(x - 2)$ oe M0 for first M if $-1/5$ used as gradient even if 5 seen first; second M still available if earned
---	--------------	--	--

4	$(7/11, 24/11)$ oe www	3 B2 for one coord correct; condone not expressed as coords, isw or M1 for subst or elimination; eg $x + 2(5x - 1) = 5$ oe; condone one error SC2 for mixed fractions and decimals eg $(3.5/5.5, 12/5.5)$	
---	------------------------	--	--

5	<p>(i) $\frac{1}{2} \times x \times (x + 2 + 3x + 6)$ oe</p> <p>$x(4x + 8) = 140$ oe and given ans $x^2 + 2x - 35 = 0$ obtained correctly with at least one further interim step</p>	<p>M1</p> <p>A1</p>	<p>correct statement of area of trap; may be rectangle \pm triangle, or two triangles</p>	<p>eg $2x(x + 2) + \frac{1}{2} \times 2x \times (2x + 4)$</p> <p>condone missing brackets for M1; condone also for A1 if expansion is treated as if they were there</p>
	<p>(ii) [AB 1 www</p>	<p>3</p>	<p>or B2 for $x = [-7 \text{ or }] 5$ cao www or for $AB = 21$ or -15</p> <p>or M1 for $(x + 7)(x - 5) [= 0]$ or formula or completing square used eg $(x + 1)^2 - 36 [= 0]$; condone one error eg factors with sign wrong or which give two terms correct when expanded</p> <p>or M1 for showing $f(5) = 0$ without stating $x = 5$</p>	<p>may be done in (i) if not here – allow the marks if seen in either part of the image – some candidates are omitting the request in (i) and going straight to solving the equation (in which case give 0 [not NR] for (i), but annotate when the image appears again in (ii))</p> <p>5 on its own or $AB = 5$ with no working scores 0; we need to see $x = 5$</p>

6	<p>(i) $\text{grad AB} = \frac{0-6}{1-(-1)}$ oe [= -3] isw</p> <p>$\text{grad BC} = \frac{0-4}{1-13}$ oe [= 1/3] isw</p> <p>product of grads = -1 [so lines perp] stated or shown numerically</p>	<p>M1 for full marks, it should be clear that grads are independently obtained</p> <p>M1</p> <p>M1 or 'one grad is neg. reciprocal of other'</p> <p>or</p> <p>M1 for length of one side (or square of it)</p> <p>M1 for length of other two sides (or their squares) found independently</p> <p>M1 for showing or stating that Pythag holds [so triangle rt angled]</p>	<p>eg grads of -3 and 1/3 without earlier working earn M1M0</p> <p>for M3, must be fully correct, with gradients evaluated at least to -6/2 and -4/-12 stage</p> <p>$AB^2 = 6^2 + 2^2 = 40$, $BC^2 = 4^2 + 12^2 = 160$, $AC^2 = 14^2 + 2^2 = 200$</p>
6	<p>(ii) A $\sqrt{40}$ or $BC = \sqrt{160}$</p> <p>$\frac{1}{2} \times \sqrt{40} \times \sqrt{160}$ oe or ft their AB, BC</p> <p>40</p>	<p>M1</p> <p>M1 or M1 for one of area under AC (=70), under AB (=6) under BC (=24) (accept unsimplified) and M1 for their trap. - two triangles</p> <p>A1</p>	<p>allow M1 for $\sqrt{(1-(-1))^2 + (6-0)^2}$ or for $\sqrt{(13-1)^2 + (4-0)^2}$</p> <p>or for rectangle - 3 triangles method,</p> <p>$[6 \times 14 - \frac{1}{2}(2)(6) - \frac{1}{2}(4)(12) - \frac{1}{2}(2)(14)]$</p> <p>=84 - 6 - 24 - 14]</p> <p>M1 for two of the 4 areas correct and M1 for the subtraction</p>

6	<p>(iii) The subtended by diameter = 90° so i</p> <p>mid point M of AC = (6, 5)</p> <p>rad of circle = $\frac{1}{2}\sqrt{14^2 + 2^2} [=]\frac{1}{2}\sqrt{200}$ oe or equiv using r^2</p> <p>$(x - a)^2 + (y - b)^2 = r^2$ seen or $(x - \text{their } 6)^2 + (y - \text{their } 5)^2 = k$ used, with $k > 0$</p> <p>$(x - 6)^2 + (y - 5)^2 = 50$ cao</p>	<p>B1 or angle at centre = twice angle at circumf = $2 \times 90 = 180$ so i or showing BM = AM or CM, where M is midpt of AC; or showing that BM = $\frac{1}{2}$ AC</p> <p>B2 allow if seen in circle equation ; M1 for correct working seen for both coords</p> <p>M1 accept unsimplified; or eg $r^2 = 7^2 + 1^2$ or $5^2 + 5^2$; may be implied by correct equation for circle or by correct method for AM, BM or CM fit their M</p> <p>M1</p> <p>A1 or $x^2 + y^2 - 12x - 10y + 11 = 0$</p>	<p>condone 'AB and BC are perpendicular' or 'ABC is right angled triangle' provided no spurious extra reasoning</p> <p>allow M1 bod intent for AC = $\sqrt{200}$ followed by $r = \sqrt{100}$</p> <p>must be simplified (no surds)</p>
6	(iv) (11, 10)	1	

7	<p>(i) (0, -2) or 'crosses y-axis at -2' oe isw</p> <p>$(\pm 2^{\frac{1}{4}}, 0)$ oe isw</p>	<p>B1</p> <p>B2 or [when $y = 0$], [$x =$] $\pm 2^{\frac{1}{4}}$ or $\pm \sqrt{\sqrt{2}}$ or $\pm \sqrt[4]{2}$ isw</p> <p>B1 for one root correct</p>	condone $y = -2$
---	---	---	------------------

7	<p>(ii) [y =] $x^2 = x^4 - 2$ oe and rearrangement to $x^4 - x^2 - 2 [= 0]$ or $y^2 - y - 2 [=0]$</p> <p>$(x^2 - 2)(x^2 + 1) = 0$ oe in y</p> <p>$x^2 = 2$ [or -1] or $y = 2$ or -1 or ft or $x = \sqrt{2}$ or $x = -\sqrt{2}$ or ft</p> <p>$(\sqrt{2}, 2)$ and $(-\sqrt{2}, 2)$; with no other intersections given</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>B2</p>	<p>or formula or completing square; condone one error; condone replacement of x^2 by another letter or by x for 2nd M1 (but not the 3rd M1)</p> <p>dep on 2nd M1; allow inclusion of correct complex roots; M0 if any incorrect roots are included for x^2 or x</p> <p>or B1 for one of these two intersections (even if extra intersections given) or for $x = \pm\sqrt{2}$ (and no other roots) or for $y = 2$ (and no other roots), marking to candidates' advantage</p>	<p>if completing square, and haven't arranged to zero, can earn first M1 as well for an attempt such as $(x^2 - 0.5)^2 = 2.25$</p> <p>NB for second and third M: M0 for $x^2 - 2 = 0$ or $x^2 = 2$ oe straight from quartic eqn – some candidates probably thinking $x^4 - x^2$ simplifies to x^2; last two marks for roots are available as B marks</p> <p>some candidates having several attempts at solving this equation – mark the best in this particular case</p>
---	--	---	--	---

7	<p>(iii) from $x^4 - kx^2 - 2 [= 0]$:</p> <p>$k^2 + 8 > 0$ oe</p> <p>$k + \sqrt{k^2 + 8} \geq 0$ for all k</p> <p>[so there is a positive root for x^2 and hence real root for x and so intersection]</p>	<p>Allow x^2 replaced by other letters or x or from $y^2 - k^2y - 2k^2 [= 0]$</p> <p>B1 $k^4 + 8k^2 > 0$ oe</p> <p>B1 $k^2 + \sqrt{k^4 + 8k^2} > 0$ oe for all k</p> <p>[so there is a positive root for y and hence real root for x and so intersection]</p> <p>if B0B0, allow SC1 for $\frac{k \pm \sqrt{k^2 + 8}}{2}$ or $\frac{k^2 \pm \sqrt{k^4 + 8k^2}}{2}$ obtained [need not be simplified]</p>	<p>[alt methods: may use completing square to show similarly, or comment that at $x = 0$ the quadratic is above the quartic and that as $x \rightarrow \infty$, $x^4 - 2 > kx^2$ for all k]</p> <p>condone lack of brackets in $(-k)^2$</p>
---	--	---	---

8	<p>$y = 3x + c$ or $y - y_1 = 3(x - x_1)$</p> <p>$y - 5 = \text{their } m(x - 4)$ o.e.</p> <p>$y = 3x - 7$ or simplified equiv.</p>	<p>M1 allow M1 for 3 clearly stated/ used as gradient of required line</p> <p>M1 or (4, 5) subst in their $y = mx + c$; allow M1 for $y - 5 = m(x - 4)$ o.e.</p> <p>A1 condone $y = 3x + c$ and $c = -7$ or B3 www</p>
---	---	--